## Multiplying Radical Expressions


(1) Decide which expressions can be simplified.Explain how to multiply $(15 \sqrt{5}+5 \sqrt{3})(6 \sqrt{3}-2 \sqrt{5})$Calculate $(15 \sqrt{5}+5 \sqrt{3})(6 \sqrt{5}-2 \sqrt{3})$.Identify the steps of multiplication.Calculate the product.

Find the errors in the calculation.
with lots of tips, answer keys, and detailed answer explanations for all of the problems.

## Decide which expressions can be simplified.

Choose the expressions to be simplified.


## Hints for solving these problems

## 1 Decide which expressions can be simplified.

## Hint \#1

You can only combine like terms.
For example, $5 \sqrt{3}+6 \sqrt{3}=11 \sqrt{3}$, but you can't combine $5 \sqrt{3}+6 \sqrt{5}$.

## Hint \#2

For example:

$$
\begin{aligned}
2 \sqrt{5}(5 \sqrt{3}) & =2 \times 5 \times \sqrt{5} \times \sqrt{3} \\
& =10 \times \sqrt{5 \times 3} \\
& =10 \times \sqrt{15}
\end{aligned}
$$

## Hint \#3

There are just three terms which can be simplified.

## Answers and detailed answer explanations for these problems

## 1 Decide which expressions can be simplified.

Answer key: $A, B, D$

Combining like terms means that you only can add or subtract terms with the same variable and exponent:

- $a+a=2 a$
- $a^{2}+a^{2}=2 a^{2}$

But $a+a^{2}$ can't be simplified any further, for instance.

Let's have a look at the following example:
$(15 \sqrt{5}+5 \sqrt{3})(3 \sqrt{2}-5 \sqrt{6})$.
First we use the FOIL method:

- F multiply the first $15 \sqrt{5}(3 \sqrt{2})$
- O multiply the outer $-15 \sqrt{5}(5 \sqrt{6})$
- I multiply the inner $5 \sqrt{3}(3 \sqrt{2})$
- L multiply the last $-5 \sqrt{3}(5 \sqrt{6})$

Adding all of these resulting terms together, we get:
$(15 \sqrt{5}+5 \sqrt{3})(3 \sqrt{2}-5 \sqrt{6})=15 \sqrt{5}(3 \sqrt{2})-15 \sqrt{5}(5 \sqrt{6})+5 \sqrt{3}(3 \sqrt{2})-5 \sqrt{3}(5 \sqrt{6})$.
The radicals can be multiplied by multiplying the terms under the square roots:

- $\sqrt{5}(\sqrt{2})=\sqrt{10}$
- $\sqrt{5}(\sqrt{6})=\sqrt{30}$
- $\sqrt{3}(\sqrt{2})=\sqrt{6}$
- $\sqrt{3}(\sqrt{6})=\sqrt{18}$

So we get $(15 \sqrt{5}+5 \sqrt{3})(3 \sqrt{2}-5 \sqrt{6})=45 \sqrt{10}-75 \sqrt{30}+15 \sqrt{6}-25 \sqrt{18}$.

We are still able to simplify $\sqrt{18}=\sqrt{9 \times 2}=\sqrt{9} \times \sqrt{2}=3 \sqrt{2}$ further.
This together with the expression above gives us:

$$
(15 \sqrt{5}+5 \sqrt{3})(3 \sqrt{2}-5 \sqrt{6})=45 \sqrt{10}-75 \sqrt{30}+15 \sqrt{6}-75 \sqrt{2}
$$

And that's it! We have simplified the expression as much as we can.

